Collecting, Modeling and Predicting Human Gait Kinematics

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Collecting kinematic data



Collecting kinematic data



Collecting kinematic data









Problems:

- Expensive equipment
- An engineer needed
- A physical therapist needed
- Controlled lab environment

Therefore:

- Only a few visits in patient's life
- Function different outside of the lab







Getting the cadence





Cadence: true vs predicted



 $\rho = 0.6$

Getting the step length





Step length: true vs predicted



$$\hat{S} = 1.2H \cdot \frac{\max_t |x_{ank,L}(t) - x_{ank,R}(t)|}{\max_t |y_{ear,L}(t) - y_{ank,L}(t)|},$$

Getting the GDI





Objective:

A library for extracting meaningful biomechanic signals from videos

Modeling progression of gait pathology

Modeling progression of gait pathology

Dataset - Functional features





Dimensionality reduction



1. We reduce dimensionality using PCA.



age	PC1	PC2	PC3
5.8	33.5	-12.4	43.7
5.0	233.3	34.7	-25.4
6.9	-77.4	49.4	-67.1
9.4	29.3	8.2	-42.7
10.7	-26.2	1.8	31.6
6.3	-55.8	18.7	31.3
10.0	9.5	10.4	4.0
13.0	51.4	14.0	-4.6
5.9	47.4	18.0	0.4
9.8	35.9	21.1	-11.6
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2. We model each component as a function of age.

age	PC1	PC2	PC3	K	nee fl	exion-e	xtension	- comp	onen	it 1
5.8	33.5			500	8000					
5.0	233.3			200	-	5690 00 00	0			
6.9	-77.4				and a		0 00			
9.4	29.3			100	-	8898°	00000	0	0	
10.7	-26.2			Le			80°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°°	0		
6.3	-55.8			0 800	4			0 0		
10.0	9.5			-100				° °	0	
13.0	51.4			100	4	•890 • •8	° °	0		
5.9	47.4			-200	6.6	କ୍ଷ ଜୁଇନ୍ଟୁ ନ	0 0			
9.8	35.9				8000	0				
				-300)	20	40	60		80
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2. We model each component as a function of age.





2. We model each component as a function of age.





3. We reconstruct the process.

age	PC1	PC2	PC3
4.08	0.49	-4.47	10.21
4.16	0.48	-4.42	10.09
4.24	0.48	-4.37	9.97
4.32	0.47	-4.32	9.85
4.40	0.46	-4.26	9.73
4.48	0.46	-4.21	9.61
4.56	0.45	-4.16	9.49
4.64	0.45	-4.11	9.38
4.72	0.44	-4.06	9.26
4.80	0.44	-4.00	9.14
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Individual evolutions





Individual evolutions





Problem

Stanford University

Data:

For each patient $i \in \{1, ..., N\}$, observe n_i points $\{y_{i,1}, y_{i,2}, ..., y_{i,n_i}\}$ at age $\{t_{i,1}, t_{i,2}, ..., t_{i,n_i}\}$.

Problem:

Estimate individual curves $Y_i(t)$.



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Problem:

Estimate individual curves $Y_i(t)$.



Solution 1: Mixed-effect model

We assume

 $y_{i,\cdot} \sim \mathcal{N}(\mu_i + B_i \mathbf{w}_i, \sigma^2 I_{n_i}),$

where $\mathbf{w}_i \sim \mathcal{N}(0, \Sigma)$, $\Sigma \in \mathbb{R}^{K \times K}$.





Individual progressions

Solution 2: Low-rank model

We assume

$$y_{i,\cdot} \sim \mathcal{N}(\mu_i + B_i \mathbf{A} \mathbf{w}_i, \sigma^2 I_{n_i}),$$

where $\mathbf{w}_i \sim \mathcal{N}(0, \Sigma)$, $\Sigma \in \mathbb{R}^{D \times D}$, $A \in \mathbb{R}^{K \times D}$ and D < K.





New method based on matrix completion

Solution 3: Matrix completion

Stanford University



We want to fit

$$\sum_{i=1}^{N}\sum_{j=1}^{n_{i}}\|Y_{i}(t_{i,j})-y_{i,j}\|^{2}$$

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 Ω - set of observed indices $P_{\Omega}(\cdot)$ - projection on observed subspace $\|A\|_{F}^{2}$ - sum of squared elements $\|A\|_{*}$ - sum of singular values



Mixed-effect model



 $\underset{W}{\arg\min} \|P_{\Omega}(WB'-Y)\|_{F}^{2}$



Sparse longitudinal completion



$$rgmin_{W,A} \| P_\Omega(WA'B'-Y) \|_F^2$$



Sparse longitudinal completion



 $\underset{W,A}{\arg\min} \|P_{\Omega}(WA'B'-Y)\|_{F}^{2} + \lambda \cdot \operatorname{rank}(A)$



Sparse longitudinal completion



 $\underset{W,A}{\arg\min} \|P_{\Omega}(WA'B'-Y)\|_{F}^{2} + \lambda \|A\|_{*}$

Sparse functional PCA fit





Sparse functional PCA fit











 $\underset{W,A}{\arg\min} \|P_{[\Omega,\Omega]}(W[A'_1,A'_2]B' \otimes I_2 - [Y_1,Y_2])\|_F^2 + \|[A'_1,A'_2]\|_*$

PCA plane in OpenSim





PCA plane in OpenSim





Predicting surgical outcome

Cerebral palsy





Problem



Data:

Musculoskeletal model

Problem:

- Synthesize movement
- Approximate brain function

Problem



Data:

Musculoskeletal model

Problem:

- Synthesize movement
- Approximate brain function

Successes @ OpenAl





OpenSim in one slide



$$S_{t+1} = M(S_t, a_t),$$
 where

 S_t - state at time $t \in \{1, ..., T\}$ a_t - vector of muscle excitations M - OpenSim model





Go as far as you can minimizing the cost

$$\underset{\{a_t:t\}}{\operatorname{arg\,max}}\sum_{t=1}^{T} v(S_t) - \tilde{c}(S_t)$$

s.t.
$$\forall_t S_t = M(S_{t-1}, a_t)$$

One possible solution – policy gradient

Go as far as you can minimizing the cost

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$$\arg\max_{\theta} \sum_{t=1}^{T} v(S_t) - \tilde{c}(S_t)$$

s.t. $\forall_t S_t = M(S_{t-1}, P_{\theta}(S_{t-1}))$

Installing OpenSim with python



```
$ conda create -n opensim-rl -c kidzik osim-rl
$ source activate opensim-rl
$
$ python
> from osim.env import RunEnv
> 
> env = RunEnv(visualize=True)
> for i in range(500):
```

> observation = env.step(env.action_space.sample())

Standing





Standing penalized





Setup



State:

- Position/velocity of center of mass, toes, ankles, pelvis and head
- Joints angles/velocities/accelerations

Action:

Activation of 18 muscles

Reward:

• Net Δ of pelvis – penalty on ligament forces

Signal @ 100Hz

Walking 1 step





Walking 2 steps







The power of a **smart** crowd



NIPS 2017: Learning to Run



38.549363

87

Sat. 23 Sep 2017 11:44

03. Anton Pechenko





















chatbots

machine learning

Dueling Als compete in learning to walk, secretly manipulating images and more at NIPS

Dense but noisy



Rich but sparse



Expert but biased



One possible solution – policy gradient

- Let $P_{\theta}(s)$ be a parametric model of the policy
- Let Q(s, a) be approximation of a state-action value

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• Optimize $J(\theta) = Q(s, P_{\theta}(s))$