# Collecting, Modeling and Predicting Human Gait Kinematics 

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(D)

## Collecting

Modeling
Predicting

## Collecting kinematic data


(D)

Pelvic tilt


Pelvic obliquity


Pelvic rotation


Hip flexion


Hip adduction


Hip rotation


Knee flexion


Knee rotation


Ankle dorsiflexion


Foot progression



## Cons

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Problems:

- Expensive equipment
- An engineer needed
- A physical therapist needed
- Controlled lab environment

Therefore:

- Only a few visits in patient's life
- Function different outside of the lab
(D)


Left ankle pos



Left knee pos



Left hip pos



## Getting the cadence

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Periodogram of the left ankle


Cadence: true vs predicted


$$
\rho=0.6
$$

## Getting the step length

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$\hat{S}=1.2 H \cdot \frac{\max _{t}\left|x_{a n k}, L(t)-x_{a n k}, R(t)\right|}{\max _{t}\left|y_{e a r}, L(t)-y_{a n k, L}(t)\right|}$,

Step length: true vs predicted


$$
\rho=0.41
$$

## Getting the GDI

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## Objective:

A library for extracting meaningful biomechanic signals from videos


## Dataset - Functional features

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## Dimensionality reduction

1. We reduce dimensionality using PCA.

$\left[\begin{array}{r|rrr}\text { age } & \text { PC1 } & \text { PC2 } & \text { PC3 } \\ \hline 5.8 & 33.5 & -12.4 & 43.7 \\ 5.0 & 233.3 & 34.7 & -25.4 \\ 6.9 & -77.4 & 49.4 & -67.1 \\ 9.4 & 29.3 & 8.2 & -42.7 \\ 10.7 & -26.2 & 1.8 & 31.6 \\ 6.3 & -55.8 & 18.7 & 31.3 \\ 10.0 & 9.5 & 10.4 & 4.0 \\ 13.0 & 51.4 & 14.0 & -4.6 \\ 5.9 & 47.4 & 18.0 & 0.4 \\ 9.8 & 35.9 & 21.1 & -11.6 \\ \vdots & \vdots & \vdots & \end{array}\right]$

## Modelling

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2. We model each component as a function of age.
$\left[\begin{array}{r|rrr}\text { age } & \text { PC1 } & \text { PC2 } & \text { PC3 } \\ \hline 5.8 & 33.5 & & \\ 5.0 & 233.3 & & \\ 6.9 & -77.4 & & \\ 9.4 & 29.3 & & \\ 10.7 & -26.2 & & \\ 6.3 & -55.8 & & \\ 10.0 & 9.5 & & \\ 13.0 & 51.4 & & \\ 5.9 & 47.4 & & \\ 9.8 & 35.9 & & \\ \vdots & \vdots & & \end{array}\right]$


## Modelling

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## Modelling

3. We reconstruct the process.

$$
\left[\begin{array}{r|rrr}
\text { age } & \text { PC1 } & \text { PC2 } & \text { PC3 } \\
\hline 4.08 & 0.49 & -4.47 & 10.21 \\
4.16 & 0.48 & -4.42 & 10.09 \\
4.24 & 0.48 & -4.37 & 9.97 \\
4.32 & 0.47 & -4.32 & 9.85 \\
4.40 & 0.46 & -4.26 & 9.73 \\
4.48 & 0.46 & -4.21 & 9.61 \\
4.56 & 0.45 & -4.16 & 9.49 \\
4.64 & 0.45 & -4.11 & 9.38 \\
4.72 & 0.44 & -4.06 & 9.26 \\
4.80 & 0.44 & -4.00 & 9.14 \\
\vdots & \vdots & \vdots & \vdots
\end{array}\right]
$$

## Individual evolutions

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## Individual evolutions

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## Problem

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## Data:

For each patient $i \in\{1, \ldots, N\}$, observe $n_{i}$ points $\left\{y_{i, 1}, y_{i, 2}, \ldots, y_{i, n_{i}}\right\}$ at age $\left\{t_{i, 1}, t_{i, 2}, \ldots, t_{i, n_{i}}\right\}$.

## Problem:

Estimate individual curves $Y_{i}(t)$.


## Problem

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## Data:

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## Problem:

Estimate individual curves $Y_{i}(t)$.


Solution 1: Mixed-effect model

We assume

$$
y_{i, \cdot} \sim \mathcal{N}\left(\mu_{i}+B_{i} \mathbf{w}_{i}, \sigma^{2} I_{n_{i}}\right)
$$

where $\mathbf{w}_{i} \sim \mathcal{N}(0, \Sigma), \Sigma \in \mathbb{R}^{K \times K}$.


## Solution 2: Low-rank model

We assume

$$
y_{i, .} \sim \mathcal{N}\left(\mu_{i}+B_{i} A \mathbf{w}_{i}, \sigma^{2} I_{n_{i}}\right)
$$

where $\mathbf{w}_{i} \sim \mathcal{N}(0, \Sigma), \Sigma \in \mathbb{R}^{D \times D}$,
$A \in \mathbb{R}^{K \times D}$ and $D<K$.


## Solution 3: Matrix completion

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We want to fit

$$
\sum_{i=1}^{N} \sum_{j=1}^{n_{i}}\left\|Y_{i}\left(t_{i, j}\right)-y_{i, j}\right\|^{2}
$$



## Solution 3: Matrix completion


$\Omega$ - set of observed indices
$P_{\Omega}(\cdot)$ - projection on observed subspace
$\|A\|_{F}^{2}$ - sum of squared elements
$\|A\|_{*}$ - sum of singular values

## Solution 3: Matrix completion

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Mixed-effect model


$$
\underset{W}{\arg \min }\left\|P_{\Omega}\left(W B^{\prime}-Y\right)\right\|_{F}^{2}
$$

## Solution 3: Matrix completion

Sparse longitudinal completion

$\arg \min \left\|P_{\Omega}\left(W A^{\prime} B^{\prime}-Y\right)\right\|_{F}^{2}$
$W, A$

## Solution 3: Matrix completion

Sparse longitudinal completion

$\underset{W}{\arg \min }\left\|P_{\Omega}\left(W A^{\prime} B^{\prime}-Y\right)\right\|_{F}^{2}+\lambda \cdot \operatorname{rank}(A)$
$W, A$

## Solution 3: Matrix completion

Sparse longitudinal completion


$$
\underset{W, A}{\arg \min }\left\|P_{\Omega}\left(W A^{\prime} B^{\prime}-Y\right)\right\|_{F}^{2}+\lambda\|A\|_{*}
$$

## Sparse functional PCA fit

## Stanford

 UniversitySparse PCA


Sparse Impute


## Sparse functional PCA fit

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## Solution 3: Matrix completion

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Multivariate sparse longitudinal completion

$\underset{W, A}{\arg \min }\left\|P_{[\Omega, \Omega]}\left(W\left[A_{1}^{\prime}, A_{2}^{\prime}\right] B^{\prime} \otimes I_{2}-\left[Y_{1}, Y_{2}\right]\right)\right\|_{F}^{2}+\left\|\left[A_{1}^{\prime}, A_{2}^{\prime}\right]\right\|_{*}$

## PCA plane in OpenSim

## PCA plane in OpenSim



## Cerebral palsy

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## Problem

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## Data:

- Musculoskeletal model


## Problem:

- Synthesize movement
- Approximate brain function


## Problem

Stanford

## Data:

- Musculoskeletal model


## Problem:

- Synthesize movement
- Approximate brain function


## Successes @ OpenAI

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## OpenSim in one slide

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$$
\begin{gathered}
S_{t+1}=M\left(S_{t}, a_{t}\right), \\
\text { where }
\end{gathered}
$$

$S_{t}$ - state at time $t \in\{1, \ldots, T\}$
$a_{t}$ - vector of muscle excitations
M - OpenSim model

## Walking

Go as far as you can minimizing the cost

$$
\begin{aligned}
& \underset{\left\{a_{t}: t\right\}}{\arg } \max \sum_{t=1}^{T} v\left(S_{t}\right)-\tilde{c}\left(S_{t}\right) \\
& \text { s.t. } \forall_{t} S_{t}=M\left(S_{t-1}, a_{t}\right)
\end{aligned}
$$

## One possible solution - policy gradient

Go as far as you can minimizing the cost

$$
\begin{gathered}
\underset{\theta}{\arg \max } \sum_{t=1}^{T} v\left(S_{t}\right)-\tilde{c}\left(S_{t}\right) \\
\text { s.t. } \forall_{t} S_{t}=M\left(S_{t-1}, P_{\theta}\left(S_{t-1}\right)\right)
\end{gathered}
$$

## Installing OpenSim with python

```
$ conda create -n opensim-rl -c kidzik osim-rl
$ source activate opensim-rl
$
$ python
> from osim.env import RunEnv
>
> env = RunEnv(visualize=True)
> for i in range(500):
    observation = env.step(env.action_space.sample())
```


## Standing

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## Standing penalized

## Setup

## State:

- Position/velocity of center of mass, toes, ankles, pelvis and head
- Joints angles/velocities/accelerations

Action:

- Activation of 18 muscles

Reward:

- Net $\Delta$ of pelvis - penalty on ligament forces


## Signal @ 100 Hz

## Walking 1 step

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## Walking 2 steps

The power of a smart crowd


# NIPS 2017: Learning to Run 

## NIPS <br> 2017

Reinforcement learning environments with musculoskeletal models

| 25 | 45444 | 428 | 1596 |
| :--- | :--- | :--- | :--- |
| Days left | Views | Participants | Submissions |












Unlocking the mysteries of the brain and behavior


## Z NVIDIA DEVELOPER

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kidzik / packag

Conda
$\stackrel{\wedge}{\wedge} 20132$ total downloads

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## NVIDIA Sponsors "Learning to Run" AI Competition at NIPS 2017

September 8, 2017
Participants in the Neural Information Processing Systems (NIPS) conference
"Learning to Run" competition are vying for the chance to win an NVIDIA DGX
Station, the fastest personal supercomputer for researchers and data scientists.


MONE , NEWS 4 ACALYSSS , Multrmedu > ARTCCE
Multimedia
Watch: Computer-Generated Skeletons Run for Cerebral Palsy
Tony Palions
10 Augat 2017



## chatbots

machine learning

Dueling Als compete in learning to walk, secretly manipulating images and more at NIPS

Dense but noisy


Rich but sparse
Expert but biased
Sparse Impute



## One possible solution - policy gradient

- Let $P_{\theta}(s)$ be a parametric model of the policy
- Let $Q(s, a)$ be approximation of a state-action value
- Optimize $J(\theta)=Q\left(s, P_{\theta}(s)\right)$

